



Chapter 4

Voltage, Current, and Power

Voltage and Current
Resistance and Ohm's Law
AC Voltage and Power



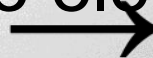
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Review of Electrical Principles

Electric current consists of the movement of charges. The charged particles in matter make currents possible.

- Nucleus made up of Protons (+) and Neutrons (no charge).
- Electrons (-) occupy clouds of probability around nucleus.
- Protons are about 1000 times bigger than electrons.

Most current is due to electron movement.



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Conductors and Insulators

Properties due to bonding (sharing) of electrons between atoms.

- Insulators – strong hold on electrons – not free to move.
- Conductors – outer electrons form a sea of electrons that are free to move within the sea.
- Semiconductors – moderate hold on electrons but electrons will break loose under right conditions.



Electrons and Fields

The moving charges which make up an electric current are usually due to electrons. Electrons and fields interact.

- Electrons in a conductor create an electric field.
- An electric field causes electrons to move or accelerate.
- Moving electrons create a magnetic field.
- A changing magnetic field causes moving electrons to accelerate or change direction.



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Basic Types of Current

Direct Current (DC)

- Electrons move in one direction.
- Can fluctuate (pulse or ripple) in magnitude, but still only in one direction.

Alternating Current (AC)

- Electrons reverse direction at a frequency.
- Current goes from zero to positive to zero to negative to zero

AC and DC may be mixed together.

AC may be sinewave, pulse, triangle, random ...



Electricity to Water Analogy

- Voltage E (Water Pressure)
- Current I (Flow of Water Molecules)
- Resistance R (Friction and obstructions)



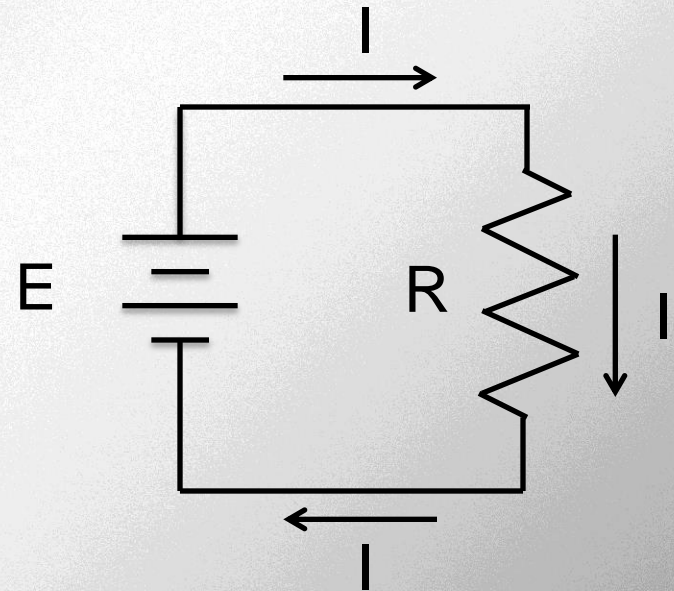
E, I, and R in a Series Circuit

A circuit is a closed path.

E represents the voltage in the circuit – a battery.

I represents the current in the circuit – the same at all points.

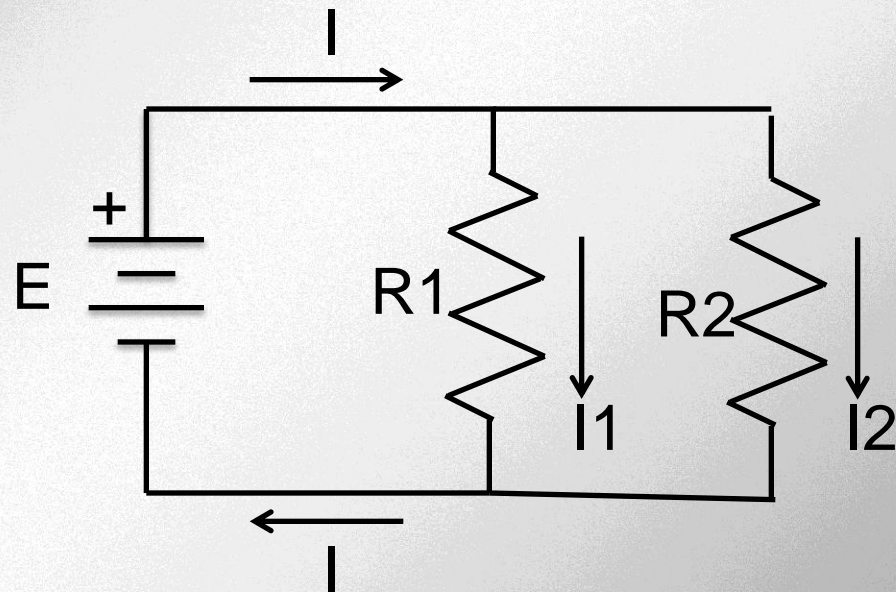
R represents the resistance of the circuit.



Currents in a Parallel Circuit

When two or more resistors are in parallel, each resistor takes part of the current I .

$I = I_1 + I_2$ is part of Kirchoff's Law.



$$I = I_1 + I_2$$



Ohm's Law ($E = I * R$)

Ohm's Law is the proportional relationship between Voltage and Current.

Current is proportional to diameter of conductor but inversely proportional to length of conductor.

- Larger conductor – More current for a given voltage.
- Longer conductor – More voltage for same current.



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Ohm's Law

A picture to remember Ohm's Law

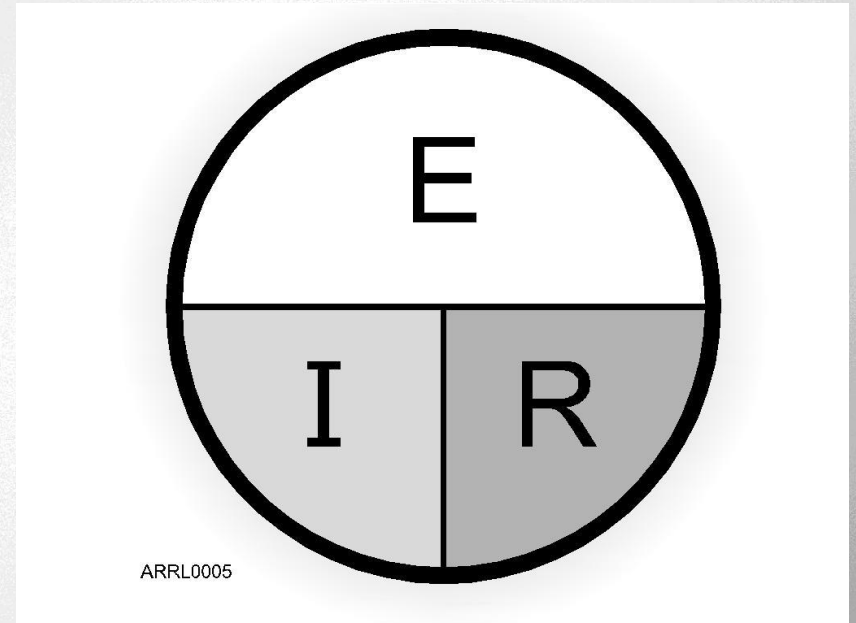
- E is voltage - Volts
- I is current - Amperes
- R is resistance - Ohms

Cover the one you don't know:

$$E = I R$$

$$I = E \text{ Over } R$$

$$R = E \text{ Over } I$$



One Ohm, one Amp, one Volt



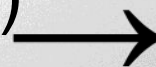
Alternating Current Defined

An Alternating Voltage reverses polarity periodically in a cycle from positive to negative.

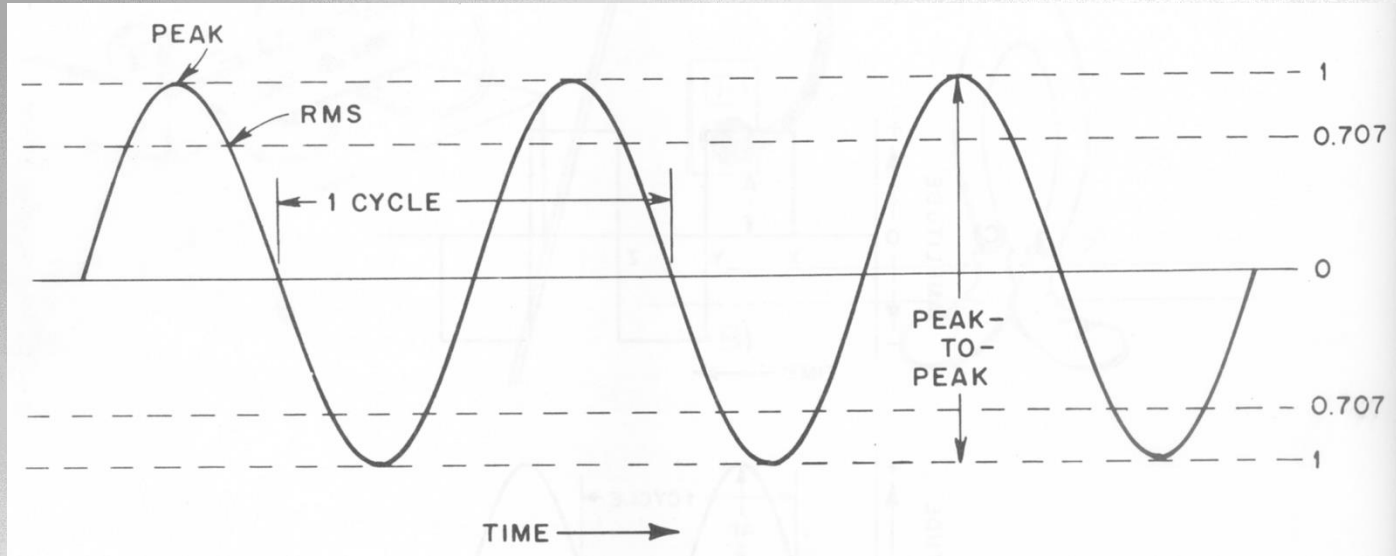
- The alternating voltage forces charges (electrons) to move back and forth through the conductor.
- The current is called Alternating Current or AC.
- The combination of a Positive period and a Negative period is called a Cycle.
- Frequency is the number of cycles in one second. (Hertz or Hz)



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AC Vocabulary



This AC Voltage is a Sine Wave.
Other AC Voltages may be rectangular or
triangular or irregular shapes.



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Electrical Power

Power (Watts) is the rate of doing work. Work is equivalent to Energy (Joules). Work is basically the effort expended to move a mass.

- Movement caused by a Force over a distance.
- Movement caused by a Pressure over a distance.

If something doesn't move, there is no work produced.

Heat produced is also a measure of work.

Power can be different at different points of a circuit.



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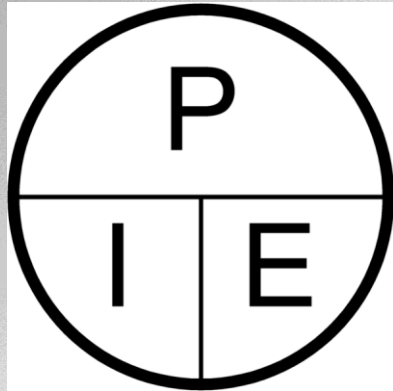
Power in Electricity

Work equals a Force times a distance moved and Power is the amount of work per second. One horsepower moves 33,000 lbs. one foot in one second.

- In a circuit, Voltage acts as the force.
- The current is the charge moved per second.
- Power in Watts is defined as Voltage times Current. $P = I * E$; One Volt, One Amp, One Watt
- 750 Watts = 1 Horsepower



Memory Device for Power Formula



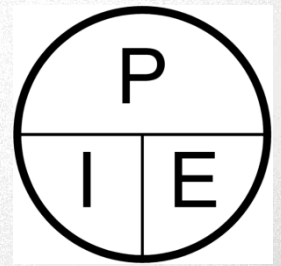
The Pie Chart – Cover the one you want.

- Cover P: $P = I * E$
- Cover I: $I = P / E$
- Cover E: $E = P / I$

One Volt, One Amp, One Watt



Other Formulas for Power



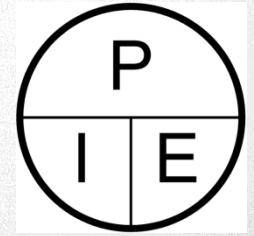
$P = I * E$ works when you know I and E . But if you only know E and R or I and R you can do some substitution.

1) $P = I * E$; 2) $E = I * R$; 3) $I = E/R$

- Substitute $I * R$ for $E \rightarrow P = I * (I * R) \rightarrow P = I^2 R$
- Substitute E/R for $I \rightarrow P = E * (E/R) \rightarrow P = E^2/R$
- Use $P = I^2 R$ when you know I and R .
- Use $P = E^2/R$ when you know E and R .



DC Power vs. AC Power



$P = I * E$ works for DC circuits where voltage and current are constant.

- 12 Volts pushing 2 Amps = 24 Watts
- 1.5 Volts pushing 300 mA = 450 mW

But in an AC circuit, the voltage and current are constantly changing.

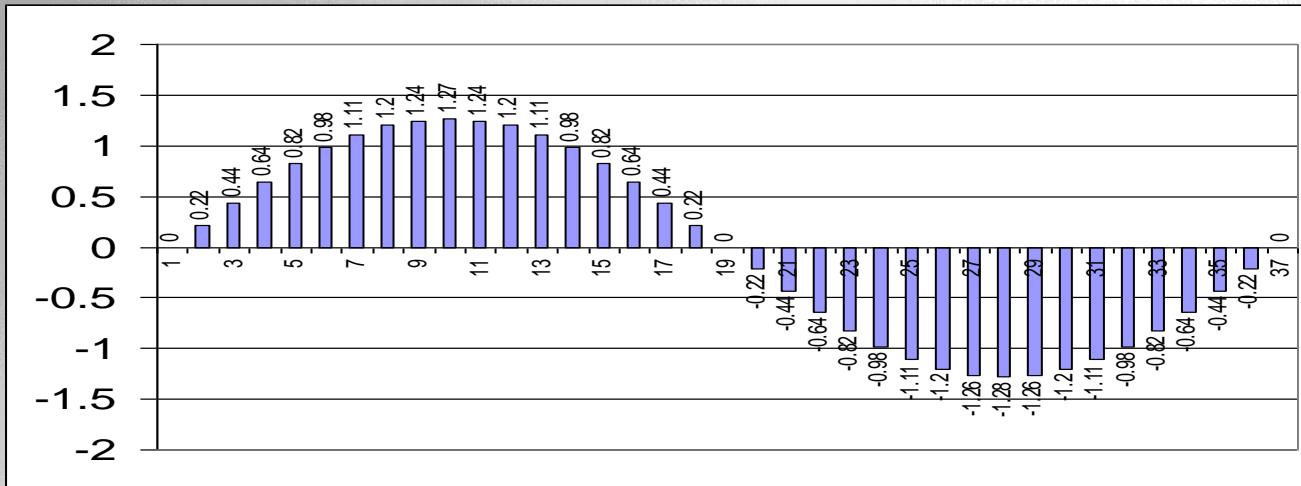
- Power at an instant is voltage at that instant times current at that instant.
- Sometimes the power is zero and sometimes it is maximum.



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Voltages at Points of a Sine Wave



- The maximum value is +1.27 V. or -1.27 V.
- The average is obtained by adding all the values and dividing by the number of values.
- Positive average will be same as negative average but different in sign.



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Average vs. Effective value of AC

For a sine wave, the mathematical average is 0.636 times the peak. (For the sine wave in the previous figure, $0.636 * 1.27 = 0.808$)

- The **effective** voltage is obtained by averaging the power over the cycle.
- But since power is proportional to the voltage squared, the power for voltages higher than average is much greater.
- Therefore the effective voltage will be higher than the average.



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RMS – Root of the Mean of the Square

Since power is proportional to V^2 , we square the individual values, add them up, take the average (mean), then take the square root of the average. This is the Root Mean Square or RMS.

RMS Formula:

$$RMS = \sqrt{\frac{\sum_{0}^N V^2}{N}}$$



RMS of a Sine Wave

The actual RMS voltage of a sine wave is 0.707 times the peak voltage.

- Remember $1 / \text{square root of } 2 = 0.707$
- The RMS voltage of a sine wave with peak voltage of $1.27 \text{ V} = 0.897\text{V}$.
- The average was 0.809 V (10% too low) which would give a power 19% low
- Power calculated from the RMS voltage is referred to as the Average Power or Power.
- Power calculated from the Average voltage usually has no meaning. →



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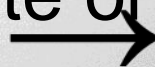
Important Points about RMS

AC RMS voltage is equivalent to a DC voltage which will do the same work.

- RMS is used in Power and Ohms Law formulas for AC voltages.
- **For Sine Waves Only**, the RMS voltage is 0.707 times the peak voltage. (!!!!)
- AC volt meters may indicate RMS voltage, but value may be wrong if wave is distorted.
- Some Digital Multimeters measure *True RMS* and are more accurate on distorted waves.



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Converting Peak Voltage to RMS

$$V_{Peak} = 1.414(V_{RMS})$$

$$V_{RMS} = \frac{V_{Peak}}{1.414} = .707(V_{Peak})$$

$$V_{P-to-P} = 2(V_{Peak})$$

Remember:

1.414 = Square root of 2

0.707 = 1 / Square root of 2



$$V_{Peak} = 1.414(V_{RMS}) \quad V_{RMS} = \frac{V_{Peak}}{1.414} = .707(V_{Peak})$$

$$V_{P-to-P} = 2(V_{Peak})$$

Calculate the missing values.

Volts _{Peak}	Volts _{Peak-to-Peak}	Volts _{RMS}
17	?	?
?	240	?
?	?	120



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Peak Envelope Power

Peak Envelope Power, PEP, is the power based on the highest Peak Voltage.

Sometimes we know the R and can measure V_{PK-PK} on an oscilloscope.

Convert Peak or Peak-to-Peak voltage to RMS.
Then:

$$PEP = \frac{(V_{RMS})^2}{R}$$

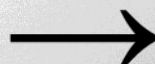


$$PEP = \frac{(V_{RMS})^2}{R}$$

$$V_{Peak} = 1.414(V_{RMS})$$

Calculate the missing values for these sine waves.

Volts _{PK - PK}	Volts _{RMS}	Load	PEP
200		50	?
?		50	1000
100		75	?



Using Decibels

Decibels (dB) are used to compare power levels and gains or losses in a system.

- Gains and losses of a system in dB are additive.
- Decibels are logarithmic.
- Matches the physical responses of hearing and sight.
- A large range of decades of values can be compared with smaller numbers, i.e., a Gain of 1,000,000 is 60dB, 1,000 is 30dB, 100 is 20dB

Commonly used to compare input to output power.

Positive → Gain; Negative → Loss.



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dB and Power Ratio Calculations

If you know the powers at two points, P2 and P1, in a system, you can calculate the gain in dB.

Gain as a ratio: $Gain = \frac{P2}{P1}$

Gain in db: $G_{db} = 10 \log_{10}(Gain)$

G_{db} to ratio: $Gain = 10^{\frac{G_{dB}}{10}} = \frac{P2}{P1}$



$$G_{db} = 10 \log_{10}(\text{Gain}) \quad \text{Gain} = 10^{\frac{G_{dB}}{10}} = \frac{P_2}{P_1}$$

P ₁	P ₂	P ₂ /P ₁	dB
25	?	+2	?
100	50	?	?
250	?	4	?
-	2000	?	9
50	500	?	?
100	1000	?	?
100	2000	?	?



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$$G_{db} = 10 \log_{10}(\text{Gain}) \quad \text{Gain} = 10^{\frac{G_{db}}{10}} = \frac{P_2}{P_1}$$

P ₁	P ₂	P ₂ /P ₁	dB
25	50	+2	3
100	50	0.5	-3
250	1000	4	6
250	2000	8	9
50	500	5	7
100	1000	10	10
100	2000	20	13

